

# On left univocal factorizations of semigroups

M. M. Miccoli,<sup>1</sup>

<sup>1</sup>Dipartimento di Matematica e Fisica, Università del Salento, Italy

Following Tolo [9], a semigroup  $S$  is said to be *factorizable* if it can be written as the set product  $AB$  of proper subsemigroups  $A$  and  $B$ . In this case, we call the pair  $(A, B)$  a *factorization* of  $S$ , with factors  $A$  and  $B$ . As in Catino [1], a factorization  $(A, B)$  of a semigroup  $S$  is called *left univocal* if  $ab = a'b'$  implies  $a = a'$ , for all  $a, a' \in A$  and  $b, b' \in B$ . There are several papers on this subject, for instance see [1–8].

The main aim of the paper is to construct a semigroup  $S$  from a given semigroups  $A$  and  $B$  in such a way that  $(A, B)$  is a left univocal factorization of  $S$  where  $A \cap B$  consists of only one element, that is right identity of  $A$  and left identity of  $B$ . The construction obtained generalizes those of Köhler [Theorem 2.1, [3]], of Krishnan [Theorem 3, [4]] on monoids and of Catino [Theorem 5, [1]] on univocal factorizations.

Details of the work can found in Ref. [10]

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